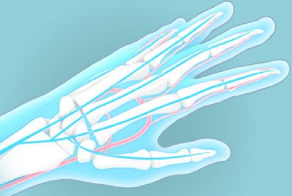


**HAND ARM  
VIBRATION**



International conference

**6-9 JUNE 2023**

Espace Prouvé,  
Nancy, France

# Determination of the Number of Measurements Required for 95% Confidence in an Upper Quartile Value of Hand-Arm Vibration Measurement Using the Monte-Carlo Method

Paul Pitts

Health and Safety Executive

UK

**RESEARCH AND  
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## Objective

To determine:

- The number of measured hand-arm vibration data sets that will provide  
an estimate of the **upper quartile value** that is  
**within 10%** of the true value **with 95% confidence**

Part of wider project on how to demonstrate vibration emission of low-vibration machines



## Method

- Use the HSE Hand-Arm Vibration Database
  - Assess how data sets could be modelled using random number data sets
- Use the Monte Carlo method
  - Generate large numbers of simulated HAV data sets with:
    - Known target upper-quartile value and variability
    - Varying numbers of sample in data set
  - Assess the computed 75<sup>th</sup> percentile values and
  - Determine how many samples are required to get within 10% of the target value.



## HAV data sets

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## HSE Hand-Arm Vibration Database

- Database interrogated in April 2020
- Machines for which:
  - more than 20 measurements on the same machine
- 135 machines
- Measurements are:
  - all real work activities
  - not multiple repeats of the same activity

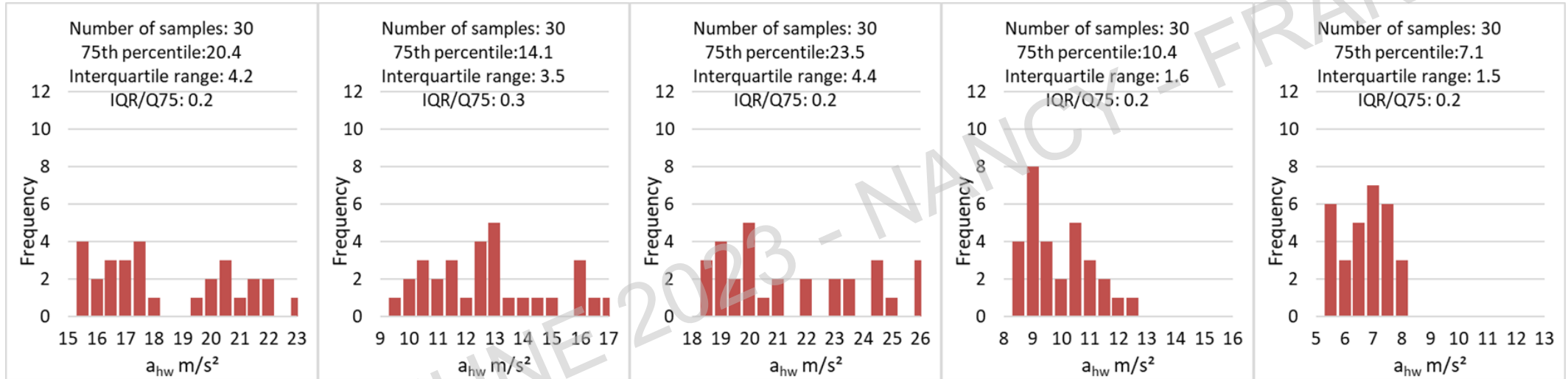


# HSE Hand-Arm Vibration Database

- Percentile statistics of the vibration total values were calculated for each of the 135 machines:
  - numbers in the data sets ranged from 21 to 216
  - median number of samples: 30
  - median 75th percentile: 11.24 m/s<sup>2</sup>
- IQR/Q75 (“*variability*”)
  - measure of variability, independent of actual vibration values
  - median IQR/Q75: 0.31 (*Range from 0.10 to 0.63*)



# Example data sets from HSE data base (sets with 30 samples)



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## Simulation of HAV data sets

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## Simulation of HAV data sets

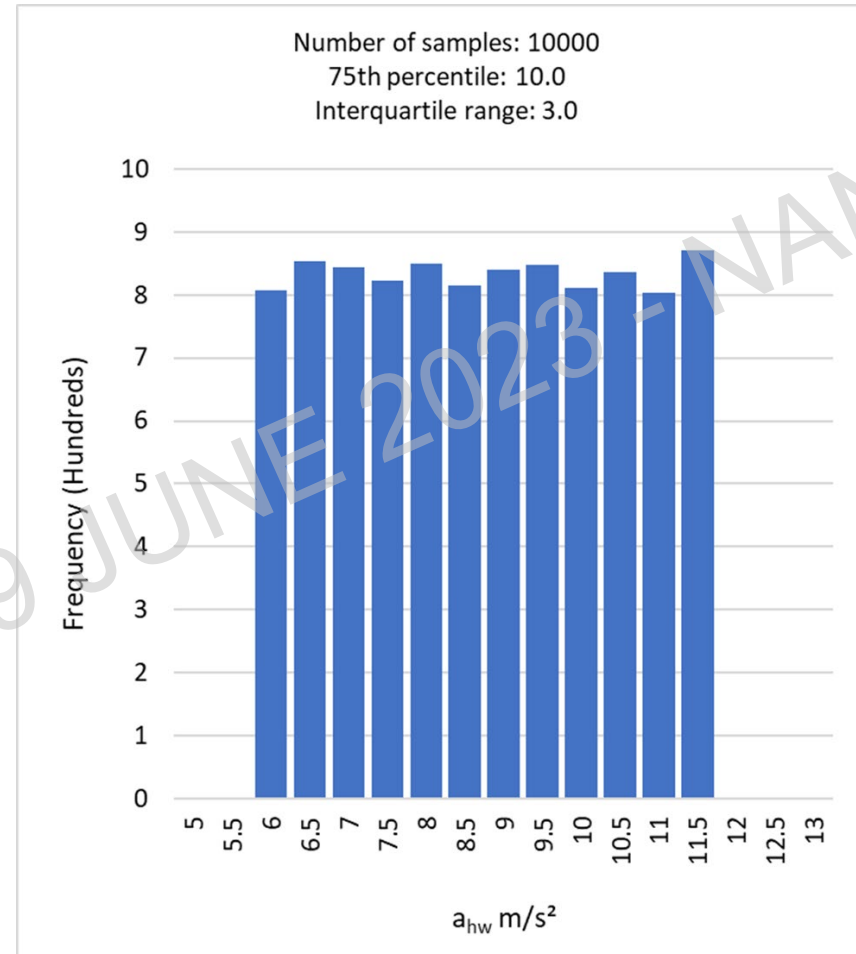
Uniform random number generator:

- Target 75th percentile (Q75): 10 m/s<sup>2</sup>
  - Median database Q75 value: 11.24 m/s<sup>2</sup>
- IQR/Q75 (“*variability*”): 0.1 to 0.6
  - Median database IQR/Q75 value: 0.31

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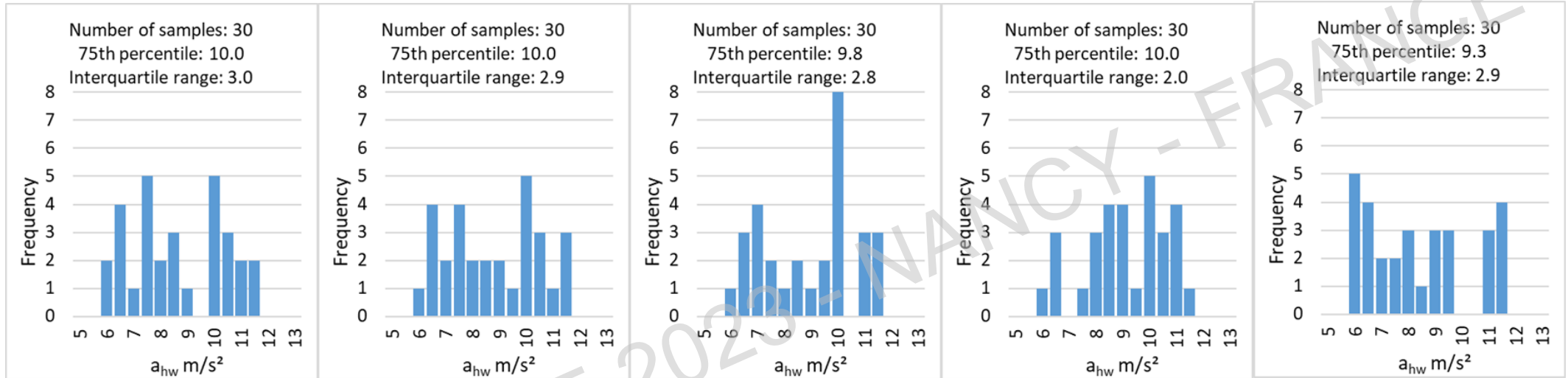
# Uniform distribution – 10,000 samples



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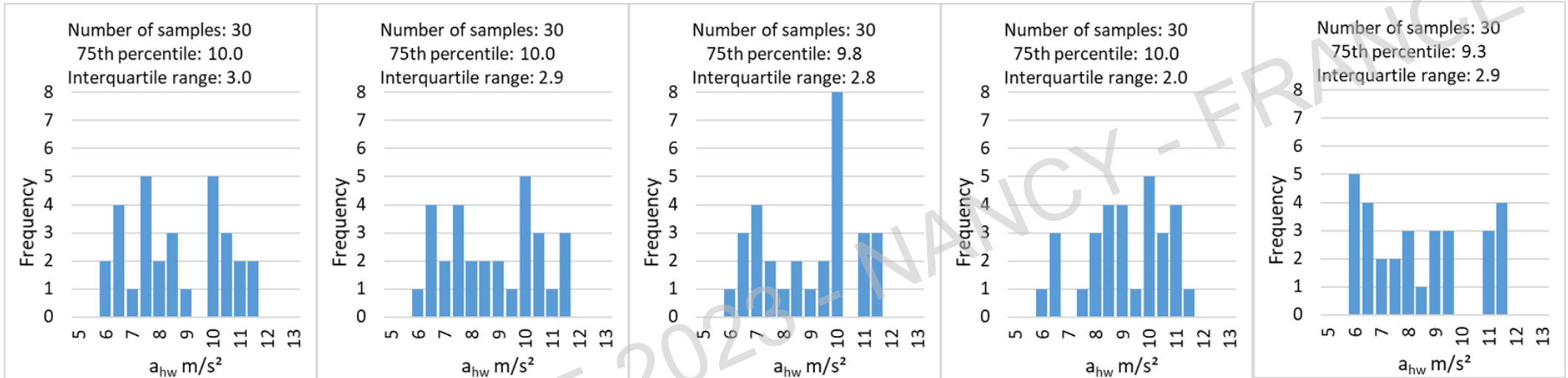
# Uniform distributions - 30 samples



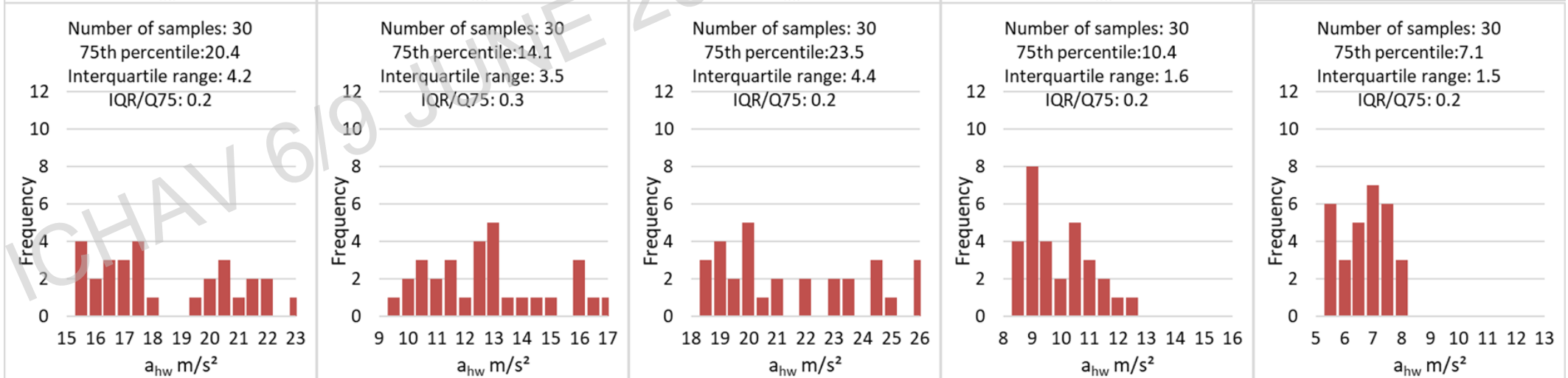
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# Comparison with real data sets

Simulated data



Real data



## Conclusion 1

The distributions from real data and simulated data are comparable, so:

- Multiple measurements of HAV on power tools may be simulated by: uniform random distributions

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## Monte Carlo Simulation

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## Monte Carlo simulation

Generate data sets:

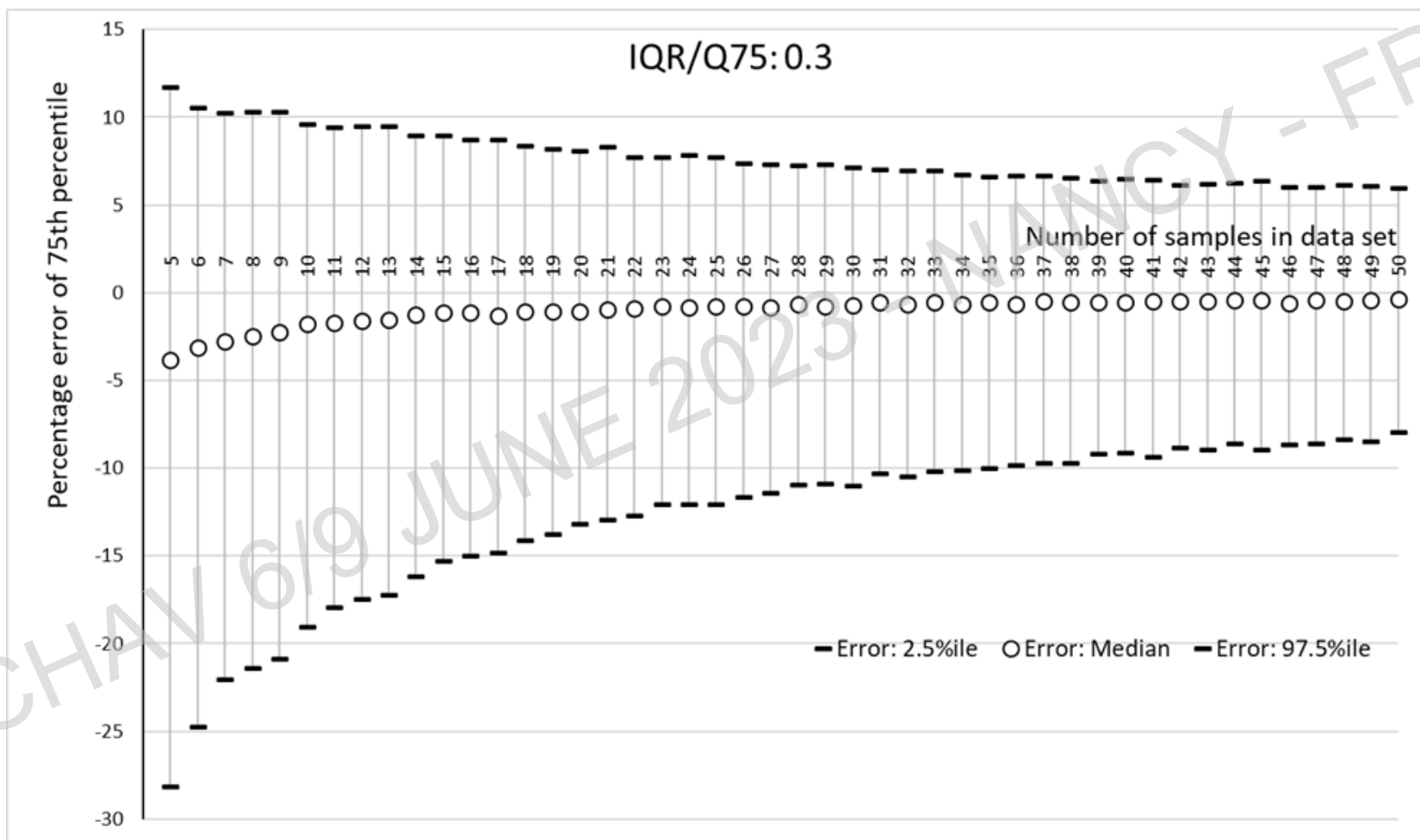
- Target 75<sup>th</sup> percentile value of **10 m/s<sup>2</sup>**
- Sample numbers: **5 to 50** (step 1)
- IRQ/Q75: **0.1, 0.2, 0.3, 0.4, 0.6**
- Generate versions of each data set **1000** times

For each set, compute:

- Q75 value
- Error from target 75<sup>th</sup> percentile
- Distribution of errors within the 1000 repeats



# Distributions of 75<sup>th</sup> percentile errors

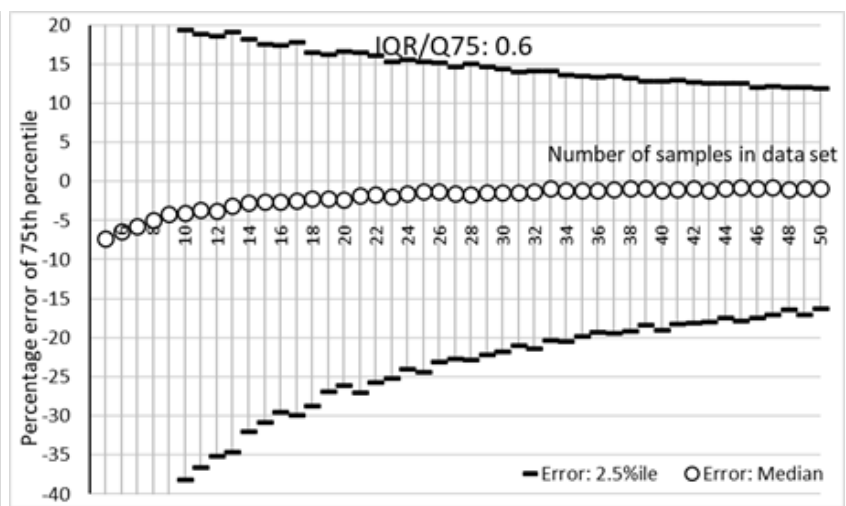
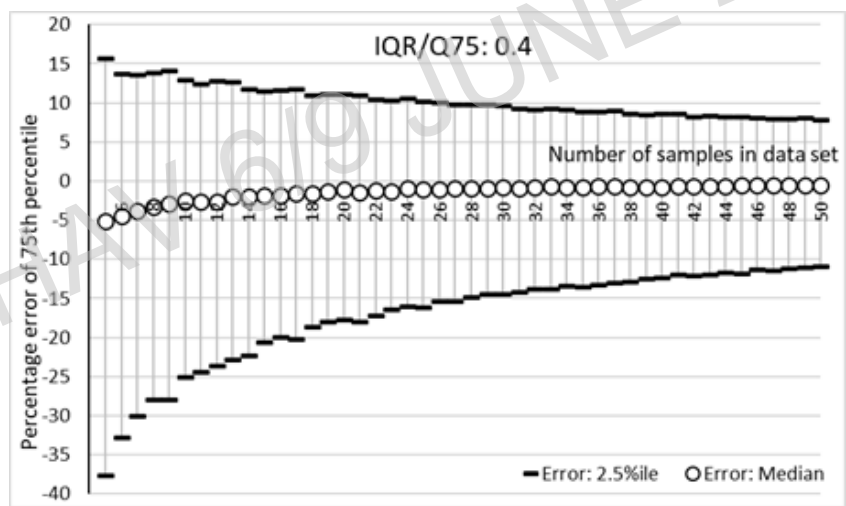
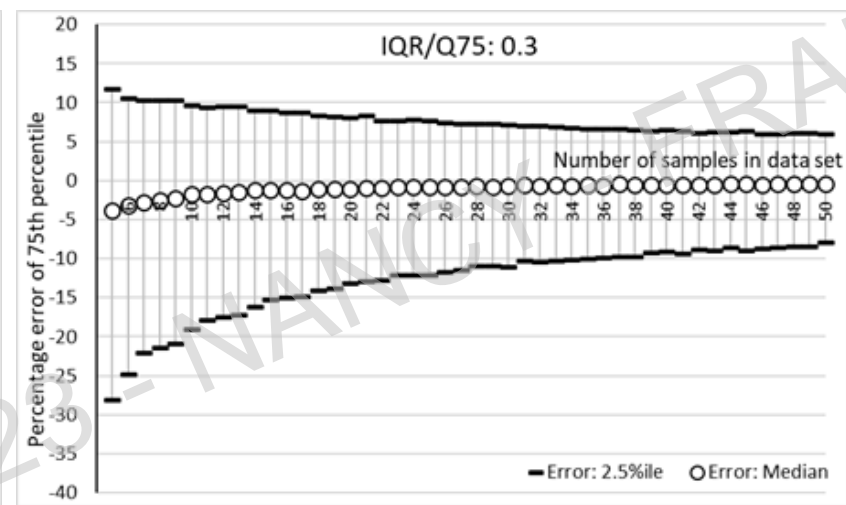
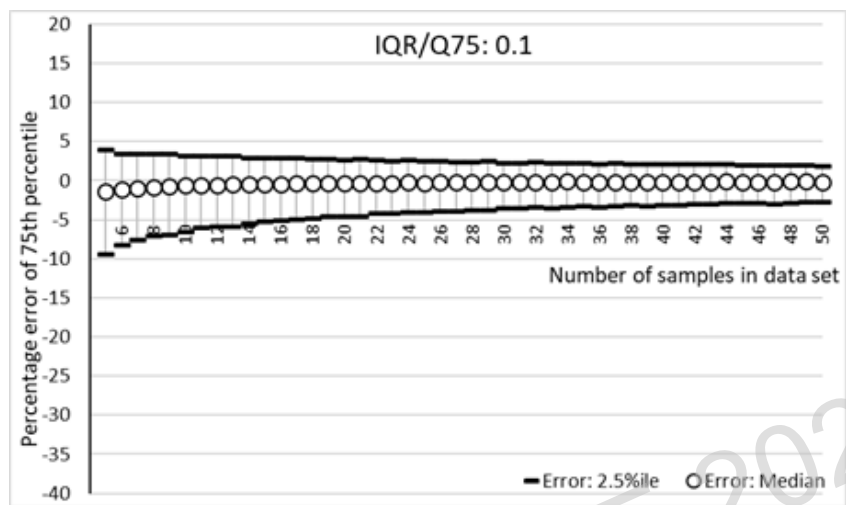


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# Distributions for different IQR/Q75 values



## Conclusions

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## Conclusion 2 & 3

For an estimates with 95% confidence:

- For data with the median variability ( $IQR/Q75 = 0.3$ ), **35 measurements** are required for an upper quartile value within **10%** of the true value.
- For data sets with greater variability ( $IQR/Q75 = 0.4$  and  $0.6$ ), between **20 and 30 measurements** are required for an upper quartile value within **20%** of the true value.



## Conclusion 4

For practical measurements:

- Between 20 and 30 measurements is likely to achieve a reliable estimate of the true upper quartile value of real-use hand-arm vibration magnitude.

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**The End**

*Thank You*

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